## Functions of functions and the exponential function math612.0 A1: From numbers through algebra to calculus and linear algebra

Gunnar Stefansson (editor) with contributions from very many students

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#### Exponential growth and decline

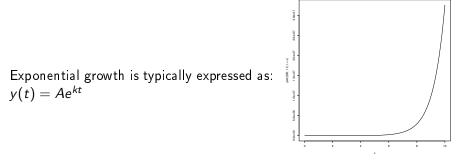


Figure: Exponential growth curve

Functions of functions and the exponential function

#### The exponential function

#### An exponential function is a function with the form: $f(x) = b^x$

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## Properties of the exponential function

Recall that the methods of the basic arithmetic implies that:

$$e^{a+b} = e^a e^b$$

for any real numbers *a* and *b*.

The exponential function  $f(x) = e^x$  is commonly written exp(x) and often has a parameter *a*, so that e.g.  $f(x) = e^{ax}$  is also called an exponential function. Note that

$$e^{bx} = (e^b)^x$$

and we can always use  $e^b x$  instead of  $a^x$  for any a>0. (TO BE COMPLETED WITH A GRAPH)

## Functions of functions

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# Storing and using R code

As R code gets more complex (more lines) it is usually stored in files. Functions are typically stored in separate files. Functions of functions and the exponential function

## Storing and calling functions in R

To save a function in a separate file use a command of the form "function.r".

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