# Functions of functions and the exponential function math612.0 A1: From numbers through algebra to calculus and linear algebra 

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## Exponential growth and decline

Exponential growth is typically expressed as: $y(t)=A e^{k t}$


Figure: Exponential growth curve

## The exponential function

An exponential function is a function with the form: $f(x)=b^{x}$

## Properties of the exponential function

Recall that the methods of the basic arithmetic implies that:

$$
e^{a+b}=e^{a} e^{b}
$$

for any real numbers $a$ and $b$.
The exponential function $f(x)=e^{x}$ is commonly written $\exp (x)$ and often has a parameter $a$, so that e.g. $f(x)=e^{a x}$ is also called an exponential function. Note that

$$
e^{b x}=\left(e^{b}\right)^{x}
$$

and we can always use $e^{b} x$ instead of $a^{x}$ for any $a>0$. (TO BE COMPLETED WITH A GRAPH)

## Functions of functions

## Storing and using R code

As R code gets more complex (more lines) it is usually stored in files. Functions are typically stored in separate files.

## Storing and calling functions in R

To save a function in a separate file use a command of the form "function.r".

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