

# Production models

fish5108statass Statistical stock assessment methods

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# History

Stock-production models: Typical for whales, shrimp, nephrops and other difficult to age species

Originally: Assumed equilibrium (oversimplified)

Now: Use dynamic stock-production models

# An equilibrium model

A simple equilibrium production model:

$$Y = rB\left(1 - \frac{B}{K}\right)$$

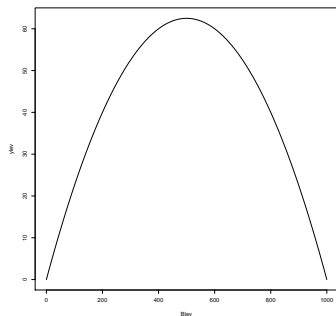


Figure : Equilibrium yield and biomass

# Simple forward projections

Given  $B$  the production is  $rB(1 - B/K)$ .

If the catch is  $Y$  the stock biomass will become

$$B + rB(1 - B/K) - Y.$$

Notably, the stock increases if  $Y$  is less than the production and vice versa.

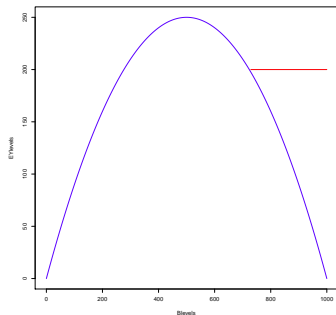


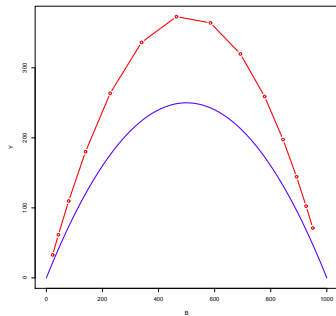
Figure : Equilibrium yield with a constant catch line.

# The problem with equilibrium models

Over-fished=catch above sustainable yield

Observed biomass and catch all above the underlying curve

Note: Will overestimate production if assume equilibrium



**Figure :** The bias issue when estimating data from an equilibrium model. The solid line is the true model and the dot/dashed line is from generated data when fishing is 1.5 times the equilibrium catch.

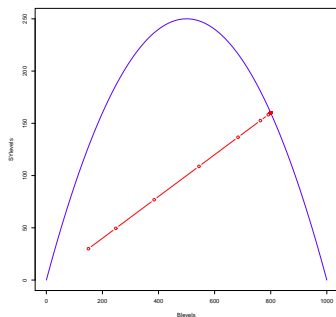
# A dynamic biomass model

A simple forward projection model:

$$B_{y+1} = B_y + rB_y(1 - B_y/K) - Y_y$$

where the catch is specified according to some rule, e.g. proportional harvest:

$$Y_y = pB_y.$$



**Figure :** Equilibrium yield and curve describing the trajectory of catch and biomass under a constant harvest strategy.

# Unknown parameters

Model:  $B_{y+1} = B_y + rB_y(1 - B_y/K) - Y_y$

Unknown parameters:  $r$ ,  $K$ , and  $B_0$ .

- Given model and parameters, the trajectory can be generated.
- Assumes catches are known constants (no error)
- Parsimony: May (need to) assume  $B_0 = K$ .